



Improving Information Cascade Modeling by Social Topology and Dual Role User Dependency

Baichuan Liu[§][0000-0002-6216-3011], Deqing Yang^{§*}[0000-0002-1390-3861],
Yuchen Shi[‡], and Yueyi Wang[‡]

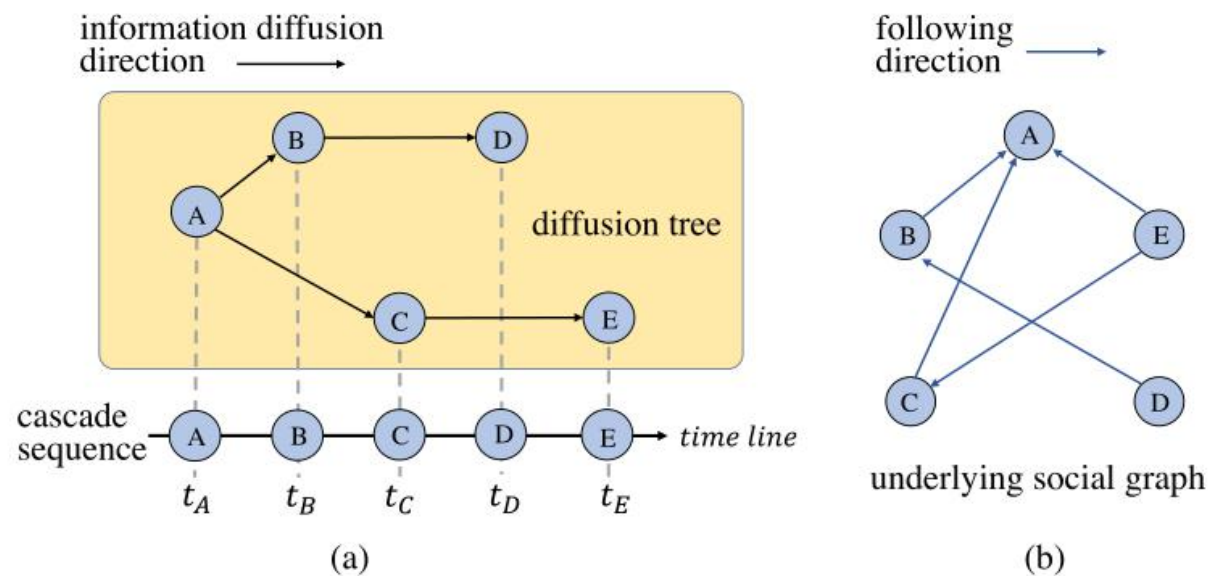
School of Data Science, Fudan University, Shanghai 200433, China.

[§]{bcliu20,yangdeqing}@fudan.edu.cn, [‡]{ycshi21,yueyiwang21}@m.fudan.edu.cn

Github:<https://github.com/JUNJINO126/TAN-DRUD>
DASFAA 2022



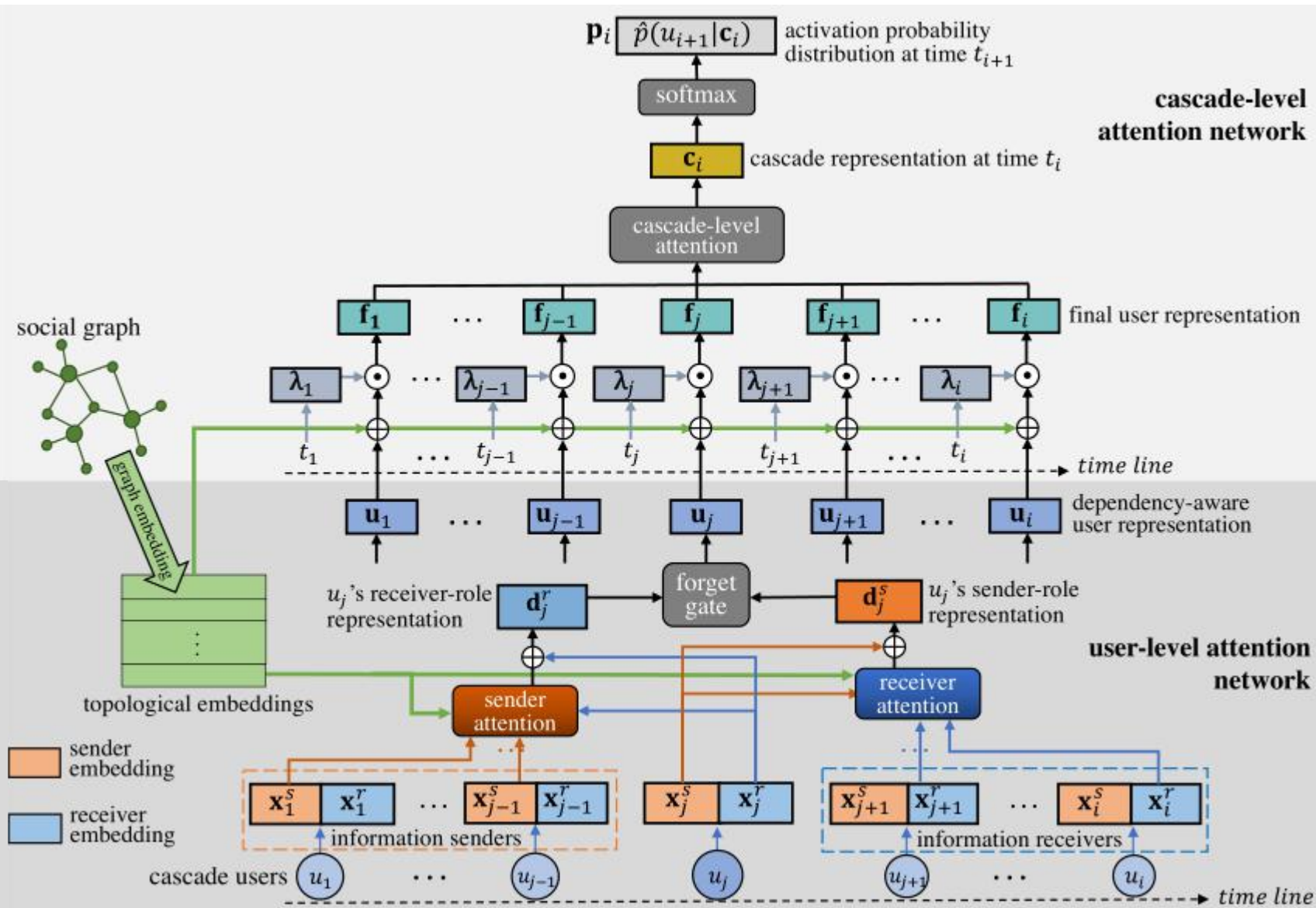
Introduction



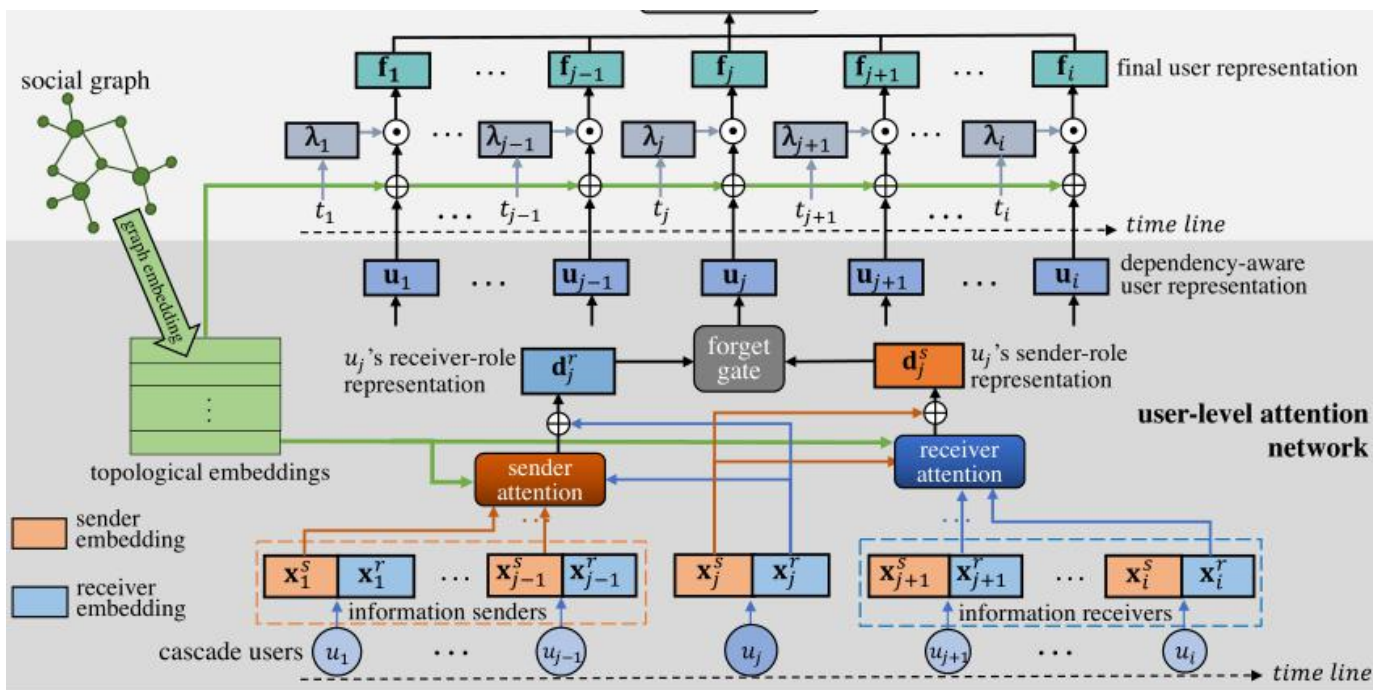
The **user dependencies** captured by most of previous diffusion models are only **unidirectional**. They suppose a successor is only influenced by a **predecessor** during information diffusion, whereas the **opposite dependency** is rarely considered

Fig. 1. An example of an information cascade sequence, diffusion tree and social graph.

Method



Method



Sender and Receiver Embeddings

$$\mathbf{X}^s, \mathbf{X}^r \in \mathbf{R}^{N \times d}$$

Social Topological Embeddings

$$\mathbf{G}_c \in \mathbf{R}^{i \times d_g}$$

User-level Attention Network

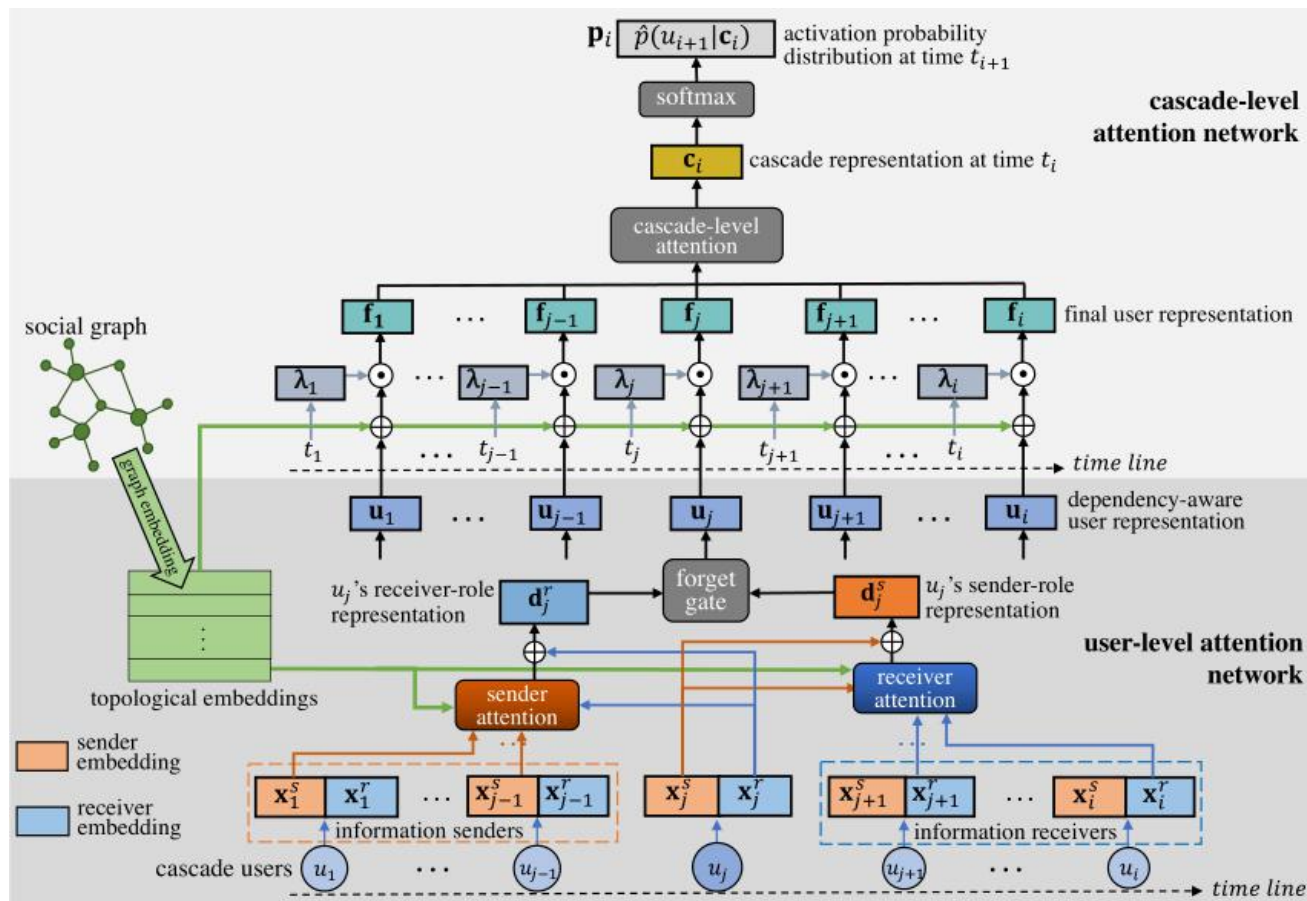
$$\alpha'_{kj} = \frac{\exp(\langle \mathbf{W}_s^o \mathbf{x}_k^s, \mathbf{W}_r^c \mathbf{x}_j^r \rangle)}{\sum_{l=1}^{j-1} \exp(\langle \mathbf{W}_s^o \mathbf{x}_l^s, \mathbf{W}_r^c \mathbf{x}_j^r \rangle)}, \quad (1)$$

$$\mathbf{E} = \frac{\mathbf{G}_c \mathbf{G}_c^T}{\|\mathbf{G}_c\| \times \|\mathbf{G}_c^T\|}, \quad (2)$$

$$\alpha_{kj}^s = \frac{\exp(\alpha'_{kj} e_{kj})}{\sum_{l=1}^{j-1} \exp(\alpha'_{lj} e_{lj})}. \quad (3)$$

$$\mathbf{d}_j^{r'} = \sum_{k=1}^{j-1} \alpha_{kj}^s \mathbf{x}_k^s, \quad \mathbf{d}_j^r = \mathbf{d}_j^{r'} + \mathbf{x}_j^r. \quad (4)$$

Method



$$\alpha'_{kj} = \frac{\exp(\langle \mathbf{W}_r^o \mathbf{x}_k^r, \mathbf{W}_s^c \mathbf{x}_j^s \rangle)}{\sum_{l=j+1}^i \exp(\langle \mathbf{W}_r^o \mathbf{x}_l^r, \mathbf{W}_s^c \mathbf{x}_j^s \rangle)}, \quad (5)$$

$$\alpha_{kj}^r = \frac{\exp(\alpha'_{kj} e_{kj})}{\sum_{l=j+1}^i \exp(\alpha'_{lj} e_{lj})}, \quad (6)$$

$$\mathbf{d}'_j^s = \sum_{k=j+1}^i \alpha_{kj}^r \mathbf{x}_k^r, \quad \mathbf{d}_j^s = \mathbf{d}'_j^s + \mathbf{x}_j^s. \quad (7)$$

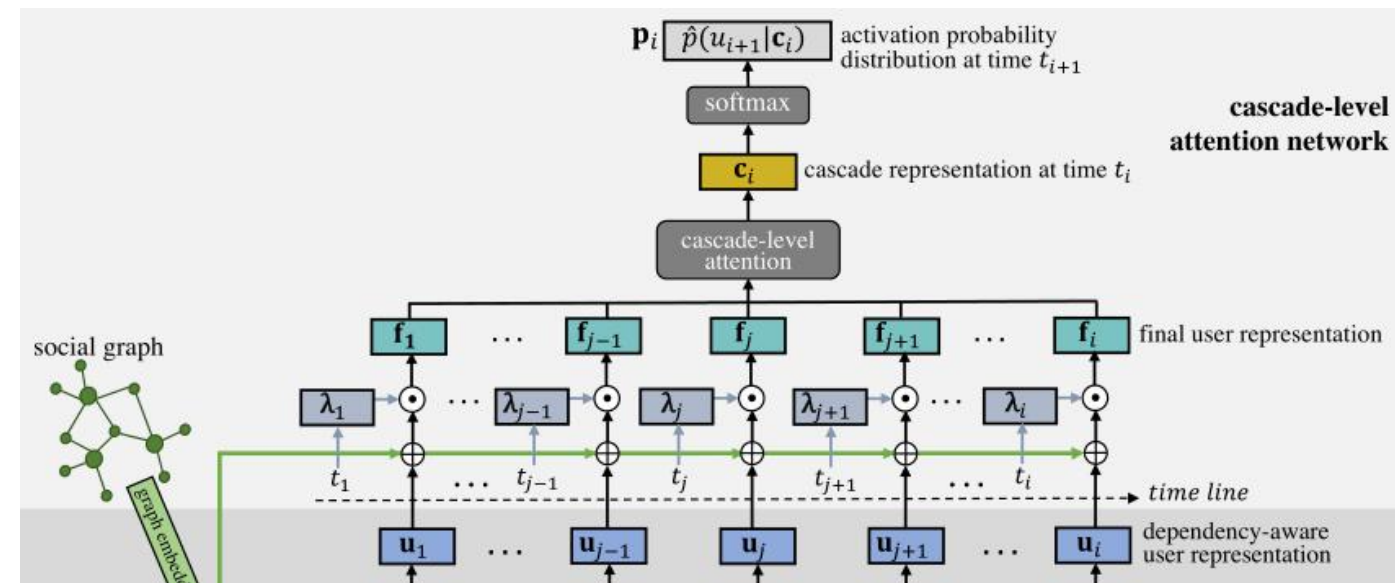
$$\mathbf{m} = \sigma(\mathbf{W}_m^s \mathbf{d}_j^s + \mathbf{W}_m^r \mathbf{d}_j^r + \mathbf{b}_m), \quad (8)$$

$$\mathbf{n} = \sigma(\mathbf{W}_n^s \mathbf{d}_j^s + \mathbf{W}_n^r \mathbf{d}_j^r + \mathbf{b}_n), \quad (9)$$

$$\mathbf{u}_j = (\mathbf{1} - \mathbf{m}) \odot \mathbf{d}_j^s + (\mathbf{1} - \mathbf{n}) \odot \mathbf{d}_j^r \quad (10)$$

Method

Cascade-level Attention Network



Prediction and Optimization

$$\mathbf{p}_i = \text{softmax}(\mathbf{W}_c \mathbf{c}_i + \mathbf{b}_c) \quad (16)$$

$$\mathcal{L} = -\frac{1}{M} \sum_{m=1}^M \sum_{i=1}^{n_m-1} \log \hat{p}(u_{i+1} | \mathbf{c}_i^m) + \lambda L_2 \quad (17)$$

$$\mathbf{G}_{new} = \tanh(\mathbf{W}_g \mathbf{G}_c + \mathbf{b}_g) \quad (11)$$

$$\Delta^t = T_{\max}/T, \quad \Delta t_j = t_i - t_j$$

$$\text{if } n = \text{int}(\Delta t_j / \Delta^t) \quad t_j^i = 1 \quad n \in [0, T)$$

$$\lambda_j = \sigma(\mathbf{W}_t \mathbf{t}_j + \mathbf{b}_t) \quad \mathbf{t}_j \in \mathbb{R}^T \quad (12)$$

$$\mathbf{f}_j = \lambda_j \odot (\mathbf{g}_j + \mathbf{u}_j) \quad (13)$$

$$\beta_j = \frac{\exp(\langle \mathbf{w}, \mathbf{f}_j \rangle)}{\sum_{k=1}^i \exp(\langle \mathbf{w}, \mathbf{f}_k \rangle)} \quad (14)$$

$$\mathbf{c}_i = \sum_{j=1}^i \beta_j \mathbf{f}_j. \quad (15)$$

Experiments

Table 1. Statistics of the three used datasets.

Dataset	Twitter	Douban	Meme
User number	12,627	23,123	4,709
Cascade number	3,442	10,602	12,661
Average cascade length	32.60	27.14	16.24
Social link number	309,631	348,280	–

Experiments

Table 2. TAN-DRUD's prediction performance (score %) with dual role embedding sizes (d).

d	RR	P@10	P@50	P@100
16	14.31	24.33	43.56	53.50
32	15.53	26.30	45.12	54.58
64	16.62	28.13	45.61	55.43
128	15.82	27.53	45.17	54.62

Table 3. TAN-DRUD's prediction performance (score %) with different time interval numbers (T).

T	RR	P@10	P@50	P@100
1	15.95	27.12	45.53	55.91
10	15.84	27.26	45.06	55.04
50	16.62	28.13	45.61	55.43
100	16.32	27.52	46.04	55.36

Experiments

Table 4. Prediction performance (score %) of all compared models for the three datasets. The best performance scores among all compared models are indicated in bold. The performance scores of leading baseline are underlined.

Dataset \ Model	Twitter				Douban				Meme			
	RR	P@10	P50	P100	RR	P@10	P@50	P@100	RR	P@10	P@50	P@100
DeepDiffuse	2.21	4.45	14.35	21.61	3.23	9.02	14.93	19.13	6.48	13.45	30.10	41.31
Bi-LSTM	7.12	13.41	26.71	36.06	7.95	15.97	29.89	37.41	12.32	24.73	46.27	56.33
Topo-LSTM	4.56	10.17	21.37	29.29	3.87	8.24	16.61	23.09	–	–	–	–
SNIDSA	–	23.37	35.46	43.39	–	11.81	21.91	28.37	–	–	–	–
FOREST	17.49	<u>24.63</u>	<u>37.73</u>	<u>46.20</u>	8.19	13.58	23.47	29.69	16.76	28.49	45.85	55.19
HiDAN	12.99	22.45	35.51	43.01	<u>8.78</u>	<u>17.40</u>	<u>32.37</u>	<u>40.49</u>	15.31	<u>29.03</u>	<u>50.01</u>	<u>60.07</u>
AN-DRUD	13.54	23.28	36.90	45.28	8.91	17.72	32.73	41.01	16.32	29.48	51.09	61.33
TAN-DRUD	16.62	28.13	45.61	55.43	9.41	18.21	34.26	42.02	–	–	–	–
improv. rate%	-4.97	14.21	20.89	19.98	7.18	4.66	5.84	3.78	-2.63	1.56	2.16	2.10



Experiments

Table 5. TAN-DRUD's prediction performance (score %) upon Twitter with different graph embedding models.

Model	RR	P@10	P@50	P@100
SDNE	16.27	26.68	41.96	51.58
LINE	15.50	26.71	43.66	53.12
DeepWalk	16.55	27.84	46.06	55.25
Node2Vec	16.62	28.13	45.60	55.43
SCE	13.59	24.20	40.54	50.75

Experiments

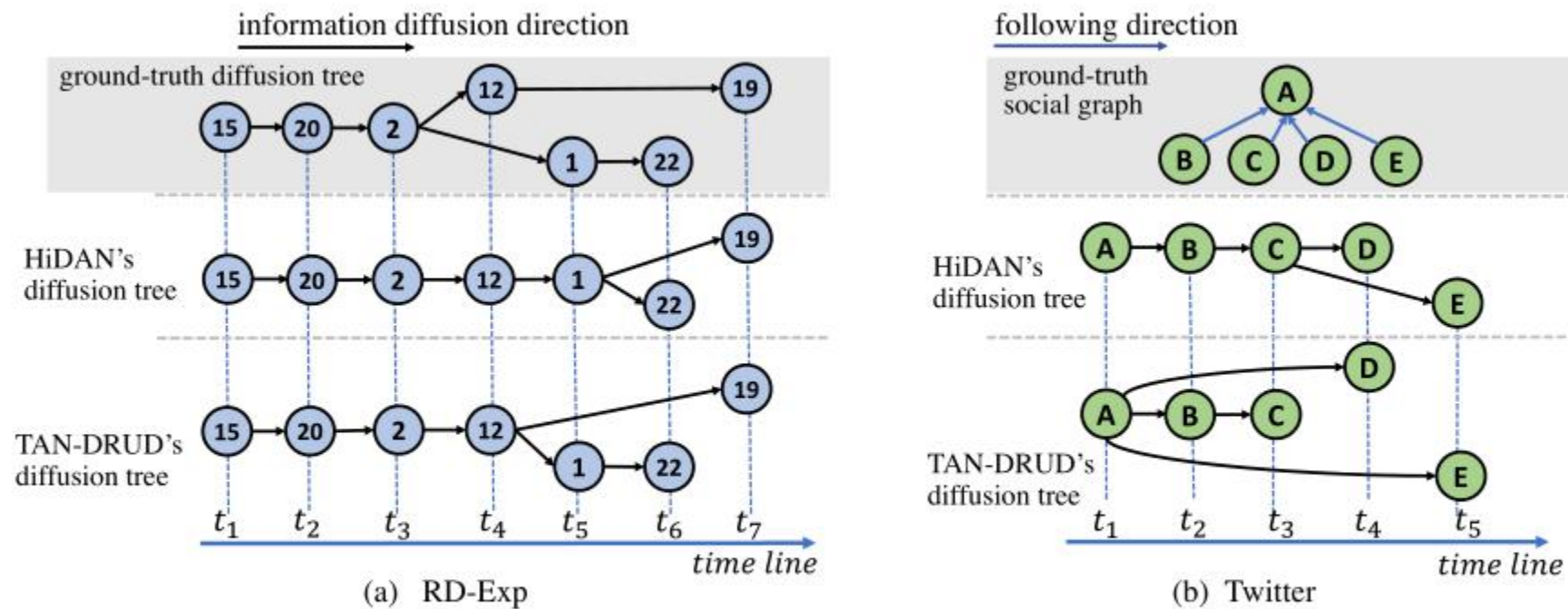


Fig. 3. Case study of diffusion tree inference.



Thanks